

Hunton & Arrathorne Community Primary School

## Progression in Written Calculations 2021+

## Calculation Policy 2022-2023

This policy supports the White Rose maths scheme used throughout the school. Progression within each area of calculation is in line with the programme of study in the 2014 National Curriculum. This calculation policy should be used to support children to develop a deep understanding of number and calculation. This policy has been designed to teach children using concrete, pictorial and abstract representations.

- Concrete representation— a pupil is first introduced to an idea or skill by acting it out with real objects. This is a 'hands on' component using real objects and is a foundation for conceptual understanding.
- Pictorial representation a pupil has sufficiently understood the 'hands on' experiences performed and can now relate them to representations, such as a diagram or picture of the problem.
- Abstract representation—a pupil is now capable of representing problems by using mathematical notation, for example 12 x 2 = 24.

It is important that conceptual understanding, supported by the use of representation, is secure for all procedures. Reinforcement is achieved by going back and forth between these representations.

Mathematics Mastery: At the centre of the mastery approach to the teaching of mathematics is the belief that all children have the potential to succeed. They should have access to the same curriculum content and, rather than being extended with new learning, they should deepen their conceptual understanding by tackling challenging and varied problems. Similarly, with calculation strategies, children must not simply rote learn procedures but demonstrate their understanding of these procedures with concrete materials and pictorial representations. This policy outlines the different calculation strategies that should be taught and used in Year 1 to Year 6 in line with the requirements of the 2014 Primary National Curriculum.

How to use the policy: This mathematics policy is a guide for all staff. All teachers have been given the scheme of work from the White Rose Maths Hub and are required to base their planning around their year group's modules and not to move onto a higher year group's scheme work. These modules use the Singapore Maths Methods and are affiliated to the workings of the 2014 Maths Programme of Study. Teachers can use any teaching resources that they wish to use and the policy does not recommend one set of resources over another, rather that, a variety of resources are used.

For each of the four rules of number, different strategies are laid out, together with examples of what concrete materials can be used and how, along with suggested pictorial representations. The principle of the concrete-pictorial-abstract (CPA) approach [Make it, Draw it, Write it] is for children to have a true understanding of a mathematical concept, they need to master all three phases within a year group's scheme of work.

Addition- EYFS			
Objectives	Concrete	Pictorial	Abstract

Knows that a group of things change in quantity when something is added.

Find the total number of items in two groups by counting all of them.

Says the number that is one more than a given number.

Finds one more from a group of up to five objects, then ten objects.

In practical activities and discussion, beginning to use the vocabulary involved in adding.

Using quantities and objects, they add two single digit numbers and count on to find the answer.

Solve problems including doubling.



Use toys and general classroom resources for children to physically manipulate, group/regroup.





etc.

counters, snap

cubes, Numicon

Use visual supports such as ten frames, part part whole and addition mats, with the physical objects and resources that can be manipulated.



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\* No expectation for children to be able to record a number sentence/addition calculation.



Start at the bigger number and counting on	Start with the larger number on the bead string and then count of to the smaller number 1 by 1 to find the answer.	12 + 5 = 17 $10  11  12  13  14  15  16  17  18  19  20$ Start at the larger number on the number line and count on in ones or in one jump to find the answer.	Place the larger number in your head and count on the smaller number to find your answer.
Regrouping to make 10 (The 'Make 10' strategy)	6+5=11 Start with the bigger number and use the smaller number to make 10. Use ten frames.	Use pictures or a number line. Regroup or Partition the smaller number using the part part whole 9 + 5 = 14	7 + 4= 11 If I am at seven, how many more do I need to make 10. How many more do I add on now?
Vocabulary	add, more, plus, and, make, alto	gether, total, equal to, equals, double, most, count on, nu	mber line, balancing, part, part, whole

	Addition- Year 2			
Objective and Strategy	Concrete	Pictorial	Abstract	
Adding 3 1-digit numbers	4 + 7 + 6= 17 Put 4 and 6 together to make 10. Add on 7. Following on from making 10, make 10 with 2 of the digits (if possible) then add on the third digit.	Image: state of the state	$\begin{array}{c} 4+7+6 = 10+7\\ 10\\ = 17 \end{array}$ Combine the two numbers that make 10 and then add on the remainder.	
Adding a 2-digit number and ones	17 + 5 = 22 Use ten frame to make 'magic ten Children explore the pattern. 17 + 5 = 22 $27 + 5 = 32$	17 + 5 = 22 Use part part whole and number line to model. 10 + 7 $10 + 7$	17 + 5 = 22	
		Bar Model	Explore related facts 17 + 5 = 22 5 + 17 = 22 22 - 17 = 5 22 - 5 = 17 22 - 5 = 17	

Adding a 2-digit number and multiples of 10	25 + 10 = 35 Explore that the ones digit does not change	27 + 30 +10 +10 +10 27 37 47 57 Base 10 may be used above the number line initially. The calculation will be shown alongside the number line to see the connection	27 + 10 = 37 27 + 20 = 47 27 + □ = 57
Adding two 2-digit numbers (No re-grouping)	24 + 15=         Add together the ones first then add the tens. Use the Base 10 blocks first before moving onto place value counters.         Image: Image	After practically using the base 10 blocks and place value counters, children can draw the counters to help them to solve additions. $\begin{array}{c} T \\ \hline \\$	$\frac{25 + 47}{20 + 5}$ $\frac{20 + 40 = 60}{5 + 7 = 12}$ $60 + 12 = 72$ Partitioning: Recording addition in columns supports place value and prepares for formal written methods with larger numbers. Toward the end of the year, children move to more formal recording using partitioning method: $40 + 7$ $\frac{30 + 5}{70 + 12}$

Vocal	bulary	/
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	Addition	- Year 3	
Objective and Strategy	Concrete	Pictorial	Abstract
Objective and Strategy Add and subtract numbers with up to 3-digits, using formal written methods of columnar addition Column addition (no regrouping)	Concrete         T       O         Using manipulatives (dienes, numicon, counters), children ine up         O       O         Concrete         Using manipulatives (dienes, numicon, counters), children ine up         O	Pictorial         Image: Constraint of the state of	Abstract 2 2 3 + 1 1 4 3 3 7 Children to move onto recording more formally. Some children may need to use the expanded method (see below).

Column addition (with regrouping)	Hundreds Tens One	Children can draw a representation of the grid to further support their	20 + 5 $40 + 8$ $60 + 13 = 73$ Children are to begin with the abstract: expanded form. For those children, that are confident
		understanding, carrying the ten underneath the line.	after AFL, the below method should be used.
	127         +         -         115         -         -         242         Exchange ten ones for a ten. Model using Dienes, Numicon and place value counters.		536 $+ 85$ $621$ $11$
Vocabulary	addition add, more, and make, sum, total, altogeth	er, double, near double, half, halve, tens bou	ndary, hundreds boundary

Addition- Year 4				
Objective and Strategy Concrete Pictorial Abstract				

Using formal written methods of columnar addition where appropriate add numbers with up to 4 digits (with exchange)	Children continue to use dienes or place value counters to add, exchanging ten ones for a ten and ten tens for a hundred hundreds thousand. The calculation will be shown alongside the manipulative used to see the connection	Children can draw a pictoral representation of the columns and place value counters to further support their learning and understanding.	Continue from previous work to carry hundreds as well as tens.
Add decimals with 2 decimal places, including money.	Introduce decimal place value counters and model exchange for addition.	2.37 + 81.79 tons on as tents hundred this 00 000 0 000 0 0000 0000 0 000 0 0 0000 0000 0 0 0	£ 2 3 · 59         + £ 7 · 55         £ 3 1 · 14         As the children move on, introduce         decimals with the same number of decimal         places and different. Money can be used         here.
Vocabulary	addition add, more, and make, sum, total, altogether, d	ouble, near double, half, halve, tens bound point	, dary, hundreds boundary, decimal, decimal

Addition- Year 5/6			
Objective and Strategy	Concrete	Pictorial	Abstract
add numbers with more than 4 digits.	See Year 4	See Year 4	Children should have abstract supported by a pictorial or concrete if needed.
add several numbers of increasing complexity, including adding money, measure and decimals with different numbers of decimal points.	See Year 4	See Year 4	8 1,059 3,668 15,301 + 20,551 120,579 1111 23 361 9 080 59 770 + 1 300 93 511 212 Insert zeros for place holders.
Vocabulary	addition add, more, and make, sum, total, alto	gether, double, near double, half, halve decimal point	e, tens boundary, hundreds boundary, decimal,

Subtraction- EYFS			
Objectives	Concrete	Pictorial	Abstract
<ul> <li>Knows that a group of things change in quantity when something is taken away</li> <li>Find one less from a group of five objects, then ten objects.</li> <li>In practical activities and discussion, beginning to use the vocabulary involved in subtracting.</li> <li>Using quantities and objects, they subtract two single digit numbers and count back to find the answer.</li> </ul>	<image/>	Image: Second	A focus on symbols and numbers to form 10-1=? $10-1=?$ $3$ $0$ $10-6=4$ $3$ $7$ $7-3=?$ $3$ $7$ $3$ $7$ $3$ $7$ $7-3=?$ $3$ $7$ $3$ $7$ $3$ $7$ $3$ $7$ $7$ $3$ $7$ $3$ $7$ $3$ $7$ $3$ $7$ $3$ $7$ $3$ $7$ $3$ $7$ $3$ $7$ $3$ $7$ $3$ $3$ $3$ $7$ $3$ $7$ $3$ $7$ $3$ $7$ $3$ $7$ $3$ $3$ $7$ $3$ $3$ $7$ $3$ $3$ $7$ $3$ $3$ $7$ $3$ $3$ $3$ $3$ $3$ $3$ $3$ $3$ $3$ $3$

	Subtro	action- Year 1	
Objective and Strategy	Concrete	Pictorial	Abstract
Subtract one-digit and two- digit numbers to 20, including 0.	Use physical objects, <u>counters</u> , cubes <u>etc</u> to show how objects can be taken away.		7—4 = 3
Taking away ones	6-4 = 2	Cross out drawn objects to show what has been taken away.	16—9 = 7
	4—2 = 2 <b>↓</b>	$ \begin{array}{c} & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & \\ & & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & $	
Counting back	Ake the larger number in your subtraction. Move the beads along your bead string as you count backwards in ones. $13 - 4$ Use counters and move them away from the group as you take ther away counting backwards as you go.         Image: Imag	$\begin{array}{c} \hline & \hline $	Put 13 in your head, count back 4. What number are you at? (Use your fingers to help you)



Vocabulary	equal to, take, take-away, less, minus, subtract, leaves, distance between, how many more, how many fewer/less than, most, least count back, how
	many left, how much less is

	Subtrac	tion- Year 2	
Objective and Strategy	Concrete	Pictorial	Abstract
Subtract a two-digit number and ones, a twodigit number and tens, two two-digit numbers Partitioning to subtract without re- Grouping: 'Friendly numbers'	34-13 = 21       Image: Constrained in the second in the sec	Children draw representations of Dienes and cross off. 1 + 1 + 2 + 2 + 2 + 2 + 2 + 2 + 2 + 2 +	43-21 = 22 Recording subtraction in columns supports place value and prepares for formal written methods with larger numbers. Toward the end of the year, children move to more formal recording using partitioning method: e.g. 43-21=22 40 and 3 : <u>20 and 1</u> <u>20 and 2</u>
Make ten strategy	34-28Use a bead bar or bead strings to model counting to next ten and the rest.	4 $4$ $4$ $4$ $4$ $4$ $4$ $4$ $3$ $90$ $93$ $93$ 'counting on' to find 'difference' Use a number line to count on to next ten and then the rest.	93—76 = 17

Vocabulary	equal to, take, take-away, less, minus, subtract, leaves, distance between, how many more, how many fewer/less than, most, least count back, how many
	left, how much less isdifference, count on, strategy, partition, tens units

	Subtraction- Year 3		
Objective and Strategy	Concrete	Pictorial	Abstract
To subtract numbers with up to three-digits, using formal written methods of columnar subtraction	47—32	Children are to be secure with use of PV counters before moving onto abstract. $ \begin{array}{c}  \hline  \hline $	Children should begin with the expanded form. Moving 47-24=23 $-\frac{40+7}{20+3}$ $\frac{728-582=146}{728}$ $\frac{728}{582}=146$ $\frac{728}{582}=146$
Column subtraction (without exchanging)	Use base 10 or Numicon to model The calculation will be shown alongside the model chosen to see the connection		onto a more formal way as below.



	Now look at the tens, can I take away 8 tens easily? I need to exchange one hundred for ten tens.
	Calculations
	00000
	Now I can take away eight tens and complete my subtraction
	Calculations
	146
	Show children how the concrete method links to the written method alongside your working. Cross out the numbers when exchanging and show where we write our new amount.
Vocabulary	equal to, take, take-away, less, minus, subtract, leaves, distance between, how many more, how many fewer/less than, most, least count back, how many left, how
	much less isdifference, count on, strategy, partition, tens units

	Subtraction- Year 4				
Objective and Strategy	Concrete	Pictorial	Abstract		
Subtract numbers with up to 4 digits using the formal written methods appropriate of columnar subtraction where appropriate Year 4 subtractraction with up to 4 digits.	Model process of exchange using Numicon, base ten and then move to PV counters. Use the phrase 'take and make' for exchange- see Y3 The calculation will be shown alongside the model chosen to see the connection <u>Model Calculation</u>	Children to draw pv counters and show their exchange—see Y3 The calculation will be shown alongside the model chosen to see the connection Model Calculation	728-582=146         * 7 '2 8         5 8 2         1 4 6         5 8 2         1 4 6         state         This will lead to an understanding of subtracting any number including decimals.		
Introduce decimal subtraction through context of money	Children to be encouraged to use counters to represent numbers and         Image: Children to represent numbers an	52.7 - 27.9 tens ones tents 00000 0000000000000000000000000000000	Adding & Subtracting Decimals. Rule 1 line 'an up! Place + 6.75 - 7195 Matters Rule 2 drop it down! No dama + 6.75 - 7195 Matters Rule 2 drop it down! No dama + 6.75 - 7.95 Matters Rule 3 fill 'an th! Thurk + 6.75 - 7.95 make + 6.75 - 7.95 make		

Vocabulary	equal to, take, take-away, less, minus, subtract, leaves, distance between, how many more, how many fewer/less than, most, least count back, how		l v many fewer/less than, most, least count back, how
many left, how much less isdifference, count on, strategy, partition, tens units			

Subtraction- Year 5/6			
Objective and Strategy	Concrete	Pictorial	Abstract

Subtract with at least 4 digits, including money and measures. Subtract with increasingly large and more complex numbers and decimal values (up to 3 decimal place).		See Year 4	$3^{10} 3^{10} 6^{10} 6^{10} 9^{10} - \frac{89,949}{60,750}$ - $36^{10} 5^{10} 5^{10} 5^{10} - \frac{36}{080} 6^{10} 8^{10} - \frac{36}{080} 8^{10} 8^{10} 8^{10} - \frac{36}{080} 8^{10} 8^{10} 8^{10} 8^{10} 8^{10} - \frac{36}{080} 8^{10} $
Vocabulary	equal to, take, take-away, less, minus, subtract, leaves, dist left, how much less isdifference, count on, strategy, part		er/less than, most, least count back, how many

	Multiplication-EYFS		
Objectives	Concrete	Pictorial	Abstract



	Multiplication- Year 1		
Objective and	Concrete	Pictorial	Abstract
Strategy			



		Use pictorial including number lines to solve problem here are 3 sweets in one bag. How many sweets are in 5 bags altogether?	
Understanding arrays	Use objects laid out in arrays to find the answers to 2 lots 5, 3 lots of 2 etc.		3 x 2 = 6 2 x 5 = 10
Vocabulary	Groups of, lots of, times, array, altogether, m	ultiply	1

	Multiplication-Year 2							
Objective and Strategy	Concrete	Pictorial	Abstract					
Counting in multiples of 2, 3, 4, 5, 10 from 0 (repeated addition)	Count the groups as children are skip counting, children may use their fin- gers as they are skip counting. Use bar models. 5+5+5+5+5+5+5=40	Number lines, counting sticks and bar models should be used to show repre- sentation of counting in multiples. (3) (3) (3) (3) (3) (3) (3) (3) (3) (3)	Count in multiples of a number aloud. Write sequences with multiples of numbers. 0, 2, 4, 6, 8, 10 0, 3, 6, 9, 12, 15 0, 5, 10, 15, 20, 25, 30 $4 \times 3 =$					
Multiplication is commutative	Create arrays using counters and cubes and Numicon.	Use representations of arrays to show different calculations and explore commutativity.	$12 = 3 \times 4$ $12 = 4 \times 3$ Use an array to write multiplication sentences and reinforce repeated addition. $00000$ $5 + 5 + 5 = 15$ $3 + 3 + 3 + 3 = 15$ $5 \times 3 = 15$ $3 \times 5 = 15$					

|--|



Vecabulary	Groups of, lots of, times, array, altogether, multiply, multiplied by, repeated addition, sets of, equal groups, times as big as, commutative, product, multiples of, scale
Vocabulary	up

Multiplication-Year 4						
Objective and Strategy	Concrete	Pictorial	Abstract			



Children can represent their work with place value counters in a way that they understand.

They can draw the counters using colours to show different amounts or just use the circles in the different columns to show their thinking as shown below.



## HTO x O

	5	7	6	11	5	X	5	3	1
5			0	3		0	0	1	X
5	2		0	5	1	0	0	5	5

Children to add up each column to find the answer.



		Multiplication Year 5	
Objective and Strategy	Concrete	Pictorial	Abstract
Multiply numbers up to 4-digits by a one-digit number using the format written method, including long multiplication for 2-digit numbers Column multiplication for 3 and 4 digits x 1 digit	Children can continue to be supported by place value counters at the stage of multipli- cation. This initially done where there is no regrouping. 321 x 2 = 642 Hundreds Tens Ones It is im- portant at this stage that they always multiply the ones first. The corresponding long multiplication is mod- elled alongside	x 300 20 7 4 1200 80 28	327 $x 4$ $28$ $80$ $1200$ $1308$ $3 2 7$ $x 4$ $1 3 0 8$ $1 2$ This may lead to a compact method.
Column multiplication (long multiplication)	Manipulatives may still be used with the corresponding long multiplication modelled alongside           Model         Calculation	Moving forward, multiply by a 2 digit number showing the different rows within the grid method. $ \begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$24 \times 6 \text{ on the first row.}$ $24 \times 6 \text{ on the first row.}$ $(6 \times 4 = 24, \text{ carrying the } 2 \text{ for the } 20, \text{ then } 6 \times 2)$ $24 \times 10 \text{ on the second row. Show multiplying by 10 by putting zero in the units first.}$ $1234$ $1234$ $16$ $7404 (1234 \times 6)$ $1234 0 (1234 \times 10)$
Vocabulary		nultiply, multiplied by, repeated addition, sets of, pairs, composite numbers, prime number, factor:	equal groups, times as big as, commutative, product, s, squared, cubed

Objective and Strategy	Concrete	Pictorial				Abst	ract
Multiply decimal up to 2 decimal place by a single digit.				s colum	ın. Lin	ne up t	gle digit belc he decimal e answer.
				3	•	1	9
			×	8			
			2	5	•	5	2

Division- EYFS							
Objectives	Concrete	Pictorial	Abstract				
<ul> <li>Solve problems including halving and sharing.</li> <li>Halving a whole, halving a quantity of objects.</li> <li>Sharing a quantity of objects.</li> <li>Sharing the state of the s</li></ul>	Children have the opportunity to physically cut objects, food or shapes in half.	<image/> <text><text><image/><image/></text></text>					


Use visual supports such as halving mats and part part whole, with the physical objects and resources that can be manipulated.



Halving Mat



Counting and other maths resources for children to explore sharing between 3 or more.

Counting and other

maths resources for share into two equal groups.

children to



	Division- Year 1				
Objective and Strategy	Concrete	Pictorial	Abstract		
Division as sharing (sharing objects into groups)	Image: Non-State of the state of the st	Children use pictures or shapes to share quantities. 3 + 2 = 4 Children use bar modelling to show and support understanding. 12 $12$ $12 + 4 = 3$	Share 9 buns between three people. 9 ÷ 3 = 3		
Vocabulary	share, share equally, one each, two each, group, groups o	of, lots of, array	·		

Division- Year 2			
Objective	Concrete	Pictorial	Abstract
and Strategy			



	Division- Year 3			
Objective and Strategy	Concrete	Pictorial	Abstract	

Division as	Use cubes, counters, objects or place value		How many groups of 6 in	
grouping	counters to aid understanding. 24 divided into groups of 6 = 4 96 + 3 = 32	Continue to use bar modelling to aid solving division problems. 20 20 $\div$ 5 = ? 5 x ? = 20	24? 24 ÷ 6 = 4	
Division with arrays	Link division to multiplication by creating an array and thinking about the number sentences that can be created. Eg 15 ÷ 3 = 5 5 x 3 = 15 15 ÷ 5 = 3 3 x 5 = 15	Draw an array and use lines to split the array into groups to make multiplication and division sentences	Find the inverse of multiplication and division sentences by creating eight linking number sentences. 7 x 4 = 28 4 x 7 = 28 28 ÷ 7 = 4 28 ÷ 4 = 7 28 = 7 x 4 28 = 4 x 7 4 = 28 ÷ 7 7 = 28 ÷ 4	



Division with a	14 ÷ 3 =	Complete written divisions and show the re-
remainder	Divide objects between groups and see how much is left over	r mainder using r. 29 ÷ 8 = 3 REMAINDER 5
		Jump forward in equal jumps on a number line then see how many more you need to jump to find a remainder.
	Use place value counters to work out 94 ÷ 4 Did you need to exchange any tens for ones? Is there a remainder?	Draw dots and group them to divide an amount and clearly show a remainder.
	29 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	(i)
	Moving on to:	Use bar models to show division with remain- ders. 10 10 10 7
/ocabulary	share share equally one each two each aroup aroups o	) of, lots of, array, divide, divided by, divided into, division, grouping, number line, left, left over, product





Division-Year 6		
Objective and Strategy	Abstract	

Long Division	Step 1 – a remainder in the ones
	h t o 0 4 1 R1
	4) 165
	4 does not go into 1 (hundred). So combine the 1 hundred with the 6 tens (160).
	4 goes into 16 four times.
	4 goes into 5 once, leaving a remainder of 1.
	th h t o 0 4 0 0 R7 8 ) 32 0 7
	8 does not go into 3 of the thousands. So combine the 3 thousands with the 2 hundreds (3,200).
	8 goes into 32 four times (3,200 + 8 = 400) 8 goes into 0 zero times (tens). 8 goes into 7 zero times, and leaves a remainder of 7. $\begin{array}{r} h \ t \ o \\ \hline 0 \ 6 \ 1 \\ \hline 4 \ \hline 2 \ 4 \ 7 \\ \hline - 4 \\ \hline 3 \end{array}$
	When dividing the ones, 4 goes into 7 one time. Multiply $1 \times 4 = 4$ , write that four under the 7, and subract. This finds us the remainder of 3.
	Check: 4 × 61 + 3 = 247
	$\begin{array}{r} \begin{array}{c} \text{th h t o} \\ 0402 \\ 4 \end{array} \\ \hline 1609 \\ \hline -8 \\ 1 \end{array}$
	When dividing the ones, 4 goes into 9 two times. Multiply 2 × 4 = 8, write that eight under the 9, and subract. This finds us the remainder of 1.
	Check: 4 × 402 + 1 = 1,609
	Step 2 – a remainder in the tens

	1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
	Two goes into 5 two times, or 5 tens + 2 = 2 whole tens but there is a remainder!	t o 2 $2)\overline{58}$ -4 1 To find it, multiply 2 × 2 = 4, write that 4 under the five, and subtract to find the remainder of 1 ten.	t o 29 2)58 $-4\downarrow$ 18 Next, drop down the 8 of the ones next to the leftover 1 ten. You combine the remainder ten with 8 ones, and get 18.
	1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
	t o 2 9 2 ) 5 8 -4 1 8	t o 29 2)58 -4 18 -18 0	2 9 2)58 <u>-4</u> 18 <u>-18</u> 0
	Divide 2 into 18. Place 9 into the quotient.	Multiply 9 × 2 = 18, write that 18 under the 18, and subtract.	The division is over since there are no more digits in the dividend. The quotient is 29.
Step 3 – a remainder in any o			

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
2)278	h t o 1 2 ) 2 7 8 -2 0	$ \begin{array}{r}             h t \circ \\             18 \\             2)278 \\             -2 \\             -2 \\           $
Two goes into 2 one time, or 2 hundreds + 2 = 1 hundred.	Multiply $1 \times 2 = 2$ , write that 2 under the two, and subtract to find the remainder of zero.	Next, drop down the 7 of the tens next to the zero.
Divide.	Multiply & subtract.	Drop down the next digit.
h t o 13 2)278 -2 07 Divide 2 into 7. Place 3 into the quotient.	h t o 13 $2\overline{)278}$ -2 07 -6 1 Multiply $3 \times 2 = 6$ , write that 6 under the 7, and subtract to find the remainder of 1 ten.	h t o 13 2)278 -2 07 -6 18 Next, drop down the 8 of the ones next to the 1 leftover ten.
1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
$     \begin{array}{r}             139 \\             2)278 \\             -2 \\             07 \\             -6 \\             18         \end{array}     $	h t o 1 3 9 2 ) 2 7 8 -2 0 7 - 6 1 8 -18 0	$ \begin{array}{r}             h t \circ \\             139 \\             2)278 \\             -2 \\             07 \\             -6 \\             18 \\             -18 \\             0         \end{array} $
Divide 2 into 18. Place 9 into the quotient.	Multiply 9 × 2 = 18, write that 18 under the 18, and subtract to find the remainder of zero.	There are no more digits to drop down. The quotient is 139.

Divide numbers up to 4 digits by a twodigit whole number using the formal written method of division	13 1 5 9 9 2 3 2 3 13 1 6 1 2 2 2 2 C
Vocabulary	share, share equally, one each, two each, group, groups of, lots of, array, divide, divided by, divided into, division, grouping, number line, left, left over, product, division facts, inverse, derive, formal written method.

## Minimal Resources required to support the CPA approach (depending on year group):

- 10 frames (including egg boxes)
- Straws/pipe cleaners
- Bead strings (to 20 and 100)
- Base 10/Dienes
- Place value grids
- Double-sided counters
- Part-part whole templates
- Place value counters (KS2)
- Multi-link cubes