

Hunton & Arrathorne Community Primary School

Progression in Written Calculations 2021+

Calculation Policy 2022-2023

This policy supports the White Rose maths scheme used throughout the school. Progression within each area of calculation is in line with the programme of study in the 2014 National Curriculum. This calculation policy should be used to support children to develop a deep understanding of number and calculation. This policy has been designed to teach children using concrete, pictorial and abstract representations.

- Concrete representation— a pupil is first introduced to an idea or skill by acting it out with real objects. This is a 'hands on' component using real objects and is a foundation for conceptual understanding.
- Pictorial representation a pupil has sufficiently understood the 'hands on' experiences performed and can now relate them to representations, such as a diagram or picture of the problem.
- \cdot Abstract representation—a pupil is now capable of representing problems by using mathematical notation, for example 12 x 2 = 24.

It is important that conceptual understanding, supported by the use of representation, is secure for all procedures. Reinforcement is achieved by going back and forth between these representations.

Mathematics Mastery: At the centre of the mastery approach to the teaching of mathematics is the belief that all children have the potential to succeed. They should have access to the same curriculum content and, rather than being extended with new learning, they should deepen their conceptual understanding by tackling challenging and varied problems. Similarly, with calculation strategies, children must not simply rote learn procedures but demonstrate their understanding of these procedures with concrete materials and pictorial representations. This policy outlines the different calculation strategies that should be taught and used in Year 1 to Year 6 in line with the requirements of the 2014 Primary National Curriculum.

How to use the policy: This mathematics policy is a guide for all staff. All teachers have been given the scheme of work from the White Rose Maths Hub and are required to base their planning around their year group's modules and not to move onto a higher year group's scheme work. These modules use the Singapore Maths Methods and are affiliated to the workings of the 2014 Maths Programme of Study. Teachers can use any teaching resources that they wish to use and the policy does not recommend one set of resources over another, rather that, a variety of resources are used.

For each of the four rules of number, different strategies are laid out, together with examples of what concrete materials can be used and how, along with suggested pictorial representations. The principle of the concrete-pictorial-abstract (CPA) approach [Make it, Draw it, Write it] is for children to have a true understanding of a mathematical concept, they need to master all three phases within a year group's scheme of work.

	А	addition- EYFS	
Objectives	Concrete	Pictorial	Abstract

- Knows that a group of things change in quantity when something is added.
- Find the total number of items in two groups by counting all of them.
- Says the number that is one more than a given number.
- Finds one more from a group of up to five objects, then ten objects.
- In practical activities and discussion, beginning to use the vocabulary involved in adding.
- Using quantities and objects, they add two single digit numbers and count on to find the answer.
- Solve problems including doubling.







Use toys and general classroom resources for children to physically manipulate, group/regroup.



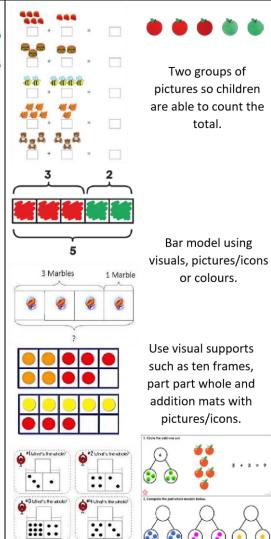
Use specific maths resources such as counters, snap cubes, Numicon etc.



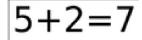


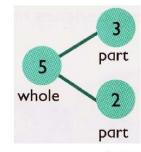


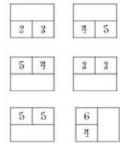
Use visual supports such as ten frames, part part whole and addition mats, with the physical objects and resources that can be manipulated.



A focus on symbols and numbers to form a calculation.





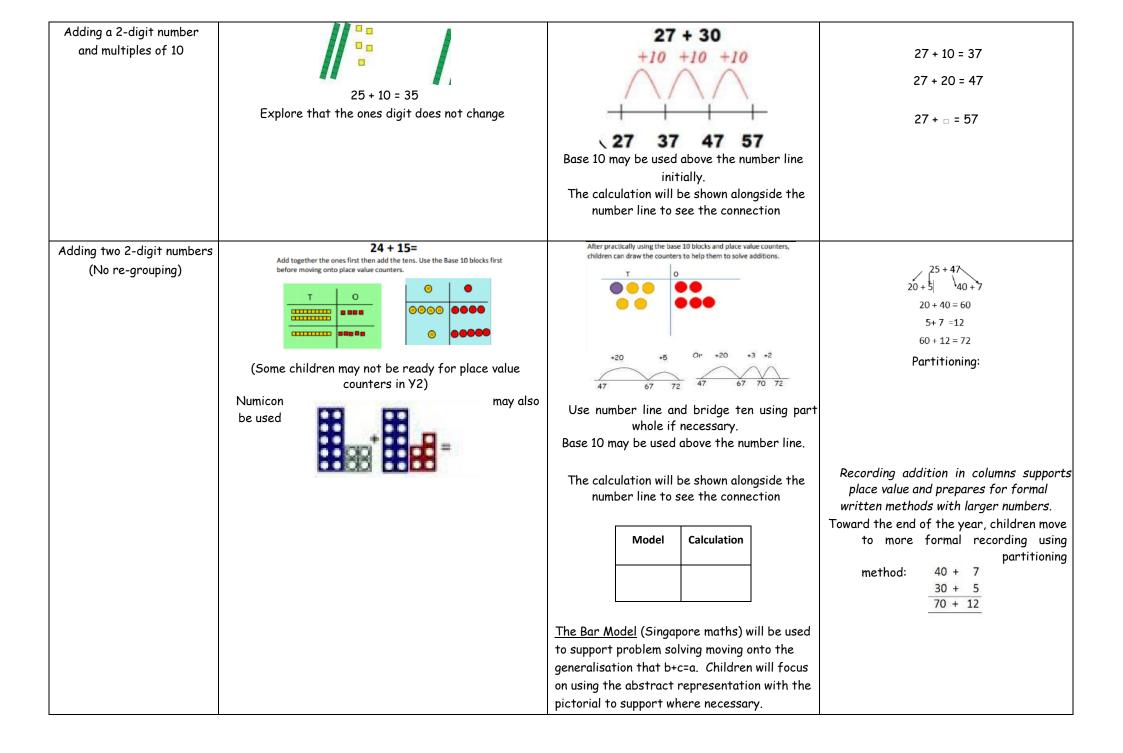


* No expectation for children to be able to record a number sentence/addition calculation.

Objective and Strategy	Concrete	Pictorial	Abstract
Combining two parts to make a whole: part- whole model	Use cubes to add two numbers together as a group or in a bar. (Some children may still need to use real objects) Use part-part whole model	The Bar Model will be continued from EYFS as a method to support problem solving involving addition, continuing with the concrete representations and moving onto using pictorial representations of objects. Some children will also move onto the abstract. Pictorial (concrete) Abstract	Use the part-part whole diagram as shown above to move into the abstract. 10=6+
Represent and use number bonds and related subtraction facts within 20	(Some children may need to initially use real objects then move onto the representation, egg boxes may also be used to support this)	6 + 4 = 10 4 + 6 = 10 10 - 4 = 6 10 - 6 = 4	10 6 4 6 + 4 = 10 4 + 6 = 10 10 - 4 = 6 10 - 6 = 4 Bar Model Bar model and part-part whole to be used alongside abstract
Addition and subtraction of one-digit and two-digit numbers to 20 including O.	**************************************	6+3=9	5 + 12 = 17 17= 12 + 5

Start at the bigger number and counting on	Start with the larger number on the bead string and then count of to the smaller number 1 by 1 to find the answer.	12 + 5 = 17 10 11 12 13 14 15 16 17 18 19 20 Start at the larger number on the number line and count on in ones or in one jump to find the answer.	Place the larger number in your head and count on the smaller number to find your answer.
Regrouping to make 10 (The 'Make 10' strategy)	Start with the bigger number and use the smaller number to make 10. Use ten frames.	Use pictures or a number line. Regroup or Partition the smaller number using the part part whole $9 + 5 = 14$ $1 $	7 + 4= 11 If I am at seven, how many more do I need to make 10. How many more do I add on now?
Vocabulary	add, more, plus, and, make, alto	gether, total, equal to, equals, double, most, count on, nu	mber line, balancing, part, part, whole

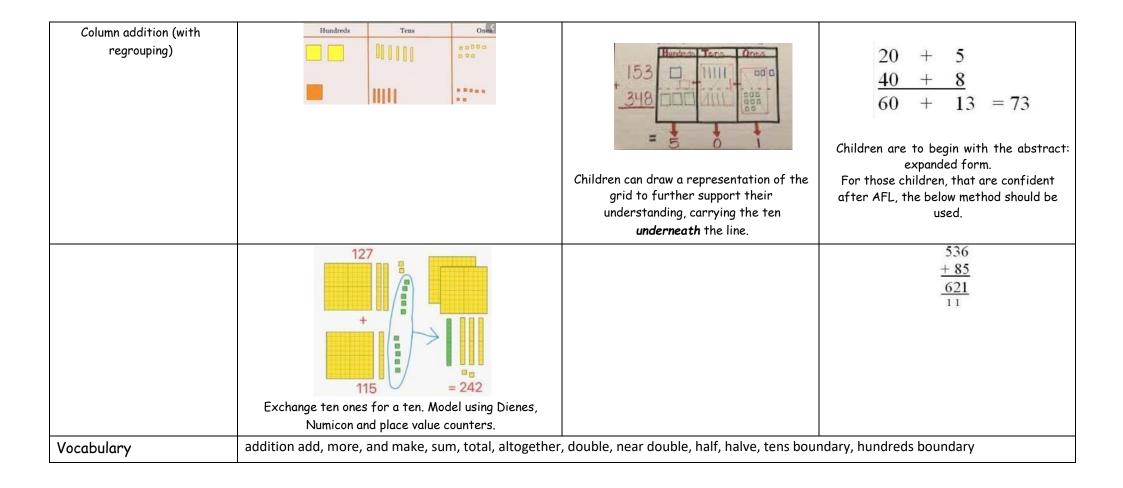
	Additio	on- Year 2	
Objective and Strategy	Concrete	Pictorial	Abstract
Adding 3 1-digit numbers	4 + 7 + 6= 17 Put 4 and 6 together to make 10. Add on 7. Following on from making 10, make 10 with 2 of the digits (if possible) then add on the third digit.	Add together three groups of objects. Draw a picture to recombine the groups to make 10.	$ \begin{array}{c} 4 + 7 + 6 = 10 + 7 \\ 10 = 17 \end{array} $ Combine the two numbers that make 10 and then add on the remainder.
Adding a 2-digit number and ones	Use ten frame to make 'magic ten Children explore the pattern. 17 + 5 = 22	17 + 5 = 22 Use part part whole and number line to model. 16 + 7 16 + 7 16 20 23	
	27 + 5 = 32	? 15 3	17 + 5 = 22
		Bar Model	Explore related facts
			17 + 5 = 22
			5 + 17 = 22
			22—17 = 5
			22-5 = 17



Vocabulary

add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line, sum, tens, units, partition, addition, column, tens boundary

	Addition	- Year 3	
Objective and Strategy	Concrete	Pictorial	Abstract
Add and subtract numbers with up to 3-digits, using formal written methods of columnar addition Column addition (no regrouping)	Using manipulatives (dienes, numicon, counters), children are to line up Children should be secure with using PV counters before moving onto pictorial. The calculation will be shown alongside the model used to see the connection Model Calculation	Children are to draw, in a PV frame, the manipulatives, that they are using. Secure knowledge of representation with the PV columns. The calculation will be shown alongside the model to see the connection Model Calculation	2 2 3 + 1 1 4 3 3 7 Children to move onto recording more formally. Some children may need to use the expanded method (see below).



	Addition-	- Year 4	
Objective and Strategy	Concrete	Pictorial	Abstract

Add decimals with 2 decimal places, including money. Introduce decimal place value counters and model exchange for addition. Vocabulary Add decimals with 2 decimal places, including money. As the children move on, introduce decimals with the same number of decimal places and different. Money can be used here. Vocabulary addition add, more, and make, sum, total, altogether, double, near double, half, halve, tens boundary, hundreds boundary, decimal, decimal point	Using formal written methods of columnar addition where appropriate add numbers with up to 4 digits (with exchange)	Children continue to use dienes or place value counters to add, exchanging ten ones for a ten and ten tens for a hundred hundreds thousand. The calculation will be shown alongside the manipulative used to see the connection Model Calculation	Children can draw a pictoral representation of the columns and place value counters to further support their learning and understanding.	3517 + 396 3913 Continue from previous work to carry hundreds as well as tens.
decimal places, including money. As the children move on, introduce decimal place value counters and model exchange for addition. Vocabulary As the children move on, introduce decimal place value counters and places and different. Money can be used here. Vocabulary addition add, more, and make, sum, total, altogether, double, near double, half, halve, tens boundary, hundreds boundary, decimal, decimal				
Introduce decimal place value counters and model exchange for addition. Vocabulary decimals with the same number of decimal places and different. Money can be used here. Vocabulary addition add, more, and make, sum, total, altogether, double, near double, half, halve, tens boundary, hundreds boundary, decimal, decimal	decimal places, including	1 1 29 20 20	tens ones tentes hundredtes	$\begin{array}{c} £23 \cdot 59 \\ +£7 \cdot 55 \\ \hline £31 \cdot 14 \end{array}$ As the children move on, introduce
		· · · · · · · · · · · · · · · · · · ·	00000 0 00000	places and different. Money can be used
	Vocabulary	addition add, more, and make, sum, total, altogether, d		lary, hundreds boundary, decimal, decimal

	Addition	1- Year 5/6	
Objective and Strategy	Concrete	Pictorial	Abstract
add numbers with more than 4 digits.	See Year 4	See Year 4	Children should have abstract supported by a pictorial or concrete if needed.
add several numbers of increasing complexity, including adding money, measure and decimals with different numbers of decimal points.	See Year 4	See Year 4	8 1,05 9 3,66 8 15,30 1 + 20,551 1 20,579 1 20,579 1 1 20,579 1 1 2 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
Vocabulary	ddition add, more, and make, sum, total, alto	gether, double, near double, half, halve decimal point	e, tens boundary, hundreds boundary, decimal,

Subtraction- EYFS

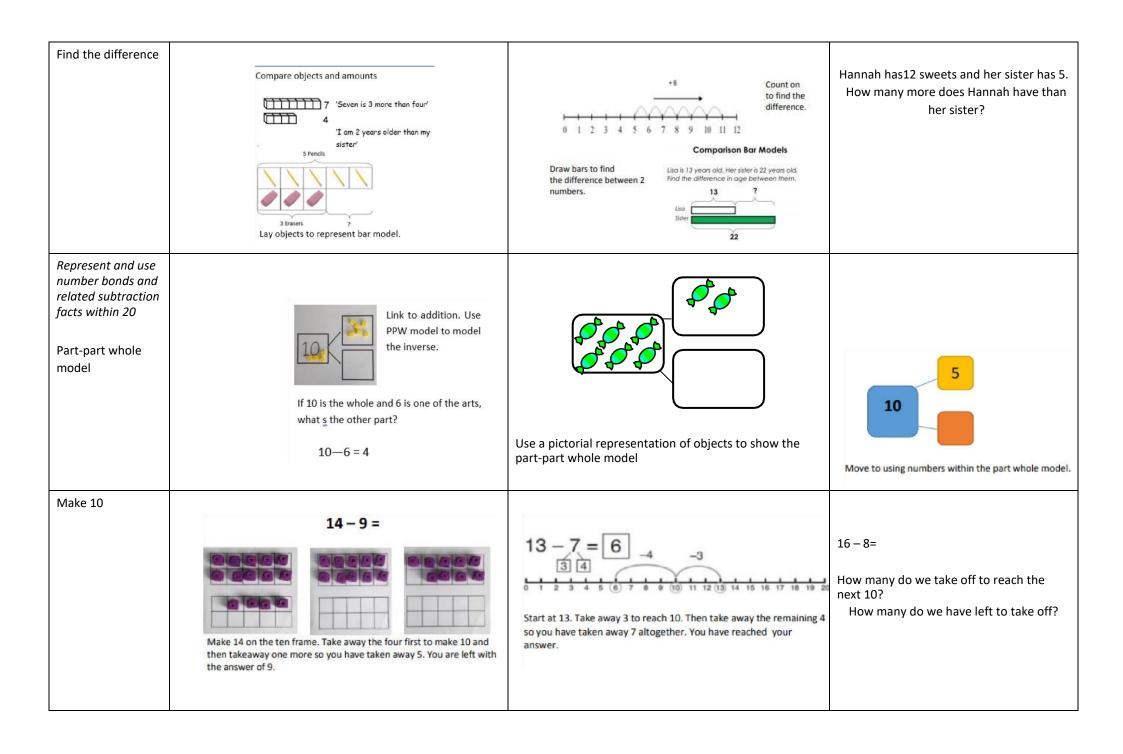
Objectives Concrete **Pictorial Abstract** Knows that a group of things change in quantity A focus on symbols when something is taken and numbers to form away 10 - 1 = ?Find one less from a group of five objects, then Use toys and general classroom resources for ten objects. children to physically manipulate, group/regroup. a calculation. In practical activities and discussion, beginning to use the 5 - 3 = vocabulary involved in A group of pictures for children to cross out subtracting. or cover quantities to support subtraction. Using quantities and objects, they subtract two single digit numbers and count back to find the answer. 3 ? Use specific maths resources such as snap cubes, Numicon, bead strings etc. 7 - 3 = ?? Use visual supports such as ten frames, part part whole and bar model with pictures/icons. Use visual supports such as ten frames, part part whole and subtraction mats, with the physical objects and resources that can be manipulated. * No expectation for children to be

able to record a number

sentence/addition calculation.

		. •	1	4
Su	btra	ction-	year	L

Objective and Strategy	Concrete	Pictorial	Abstract
Subtract one-digit and two-digit numbers to 20, including 0.	Use physical objects, counters, cubes etc to show how objects can be taken away.		7—4 = 3
Taking away ones	6—4 = 2	Cross out drawn objects to show what has been taken away.	16—9 = 7
	4-2 = 2	↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑	
Counting back	Make the larger number in your subtraction. Move the beads along your bead string as you count backwards in ones. 13 - 4	5 - 3 = 2	Put 13 in your head, count back 4. What number are you at? (Use your fingers to help you)
	Use counters and move them away from the group as you take ther away counting backwards as you go.	Count back on a number line or track Start at the bigger number and count back the smaller number showing the jumps on the number line.	



Vocabulary

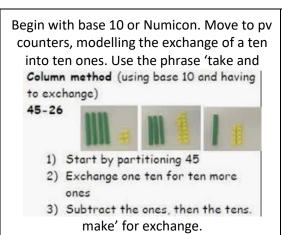
equal to, take, take-away, less, minus, subtract, leaves, distance between, how many more, how many fewer/less than, most, least count back, how many left, how much less is...

	Subtraction- Year 2				
Objective and Strategy	Concrete	Pictorial	Abstract		
Subtract a two-digit number and ones, a twodigit number and tens, two two-digit numbers Partitioning to subtract without re- Grouping: 'Friendly numbers'	Use Dienes to show how to partition the number when subtracting without regrouping. The calculation will be shown alongside the manipulative used Model Calculation	Children draw representations of Dienes and cross off. $ \begin{array}{cccccccccccccccccccccccccccccccccc$	Recording subtraction in columns supports place value and prepares for formal written methods with larger numbers. Toward the end of the year, children move to more formal recording using partitioning method: e.g. 43-21=22 40 and 3 = 20 and 1 = 20 and 2		
Make ten strategy	34—28 Use a bead bar or bead strings to model counting to next ten and the rest.	76 80 90 93 'counting on' to find 'difference' Use a number line to count on to next ten and then the rest.	93—76 = 17		

Vocabulary	equal to, take, take-away, less, minus, subtract, leaves, distance between, how many more, how many fewer/less than, most, least count back, how many
	left, how much less isdifference, count on, strategy, partition, tens units

		Subtraction- Year 3	
Objective and Strategy	Concrete	Pictorial	Abstract
To subtract numbers with up to three-digits, using formal written methods of columnar subtraction	47—32	Children are to be secure with use of PV counters before moving onto abstract. Calculations 176 - 64 = 176 - 64 112	Children should begin with the expanded form. Moving $47-24=23$ $-\frac{40+7}{20+3}$ $\frac{728-582=146}{7}$ $\frac{7}{2}$ $\frac{8}{5}$ $\frac{3}{2}$ $\frac{1}{1}$
Column subtraction (without exchanging)	The calculation will be shown alongside the model chosen to see the connection Model Calculation		onto a more formal way as below.

Column
Subtraction
(with
exchanging)



Use Base 10 to start with before moving on to place value counters. Start with one exchange before moving onto subtractions with 2 exchanges.

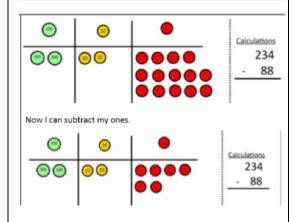
Make the larger number with the place value counters

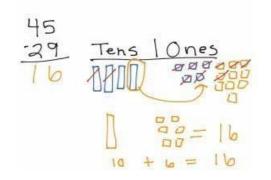
Calculations

234

- 88

Start with the ones, can I take away 8 from 4 easily? I need to exchange one of my tens for ten ones.





When confident, children can find their own way to record the exchange/regrouping

Children should begin with the expanded form. Moving

onto a more foraml way as below (bottom picture).

Now look at the tens, can I take away 8 tens easily? I need to exchange one hundred for ten tens.
©
Now I can take away eight tens and complete my subtraction
© Calculations
© 00 0 1234 - 88 146
Show children how the concrete method links to the written method alongside your working. Cross out the numbers when exchanging and show where we write our new amount.
 equal to, take, take-away, less, minus, subtract, leaves, distance between, how many more, how many fewer/less than, most, least count back, how many left, how
much less isdifference, count on, strategy, partition, tens units

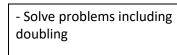
		Subtraction- Year 4	
Objective and Strategy	Concrete	Pictorial	Abstract
Subtract numbers with up to 4 digits using the formal written methods appropriate of columnar subtraction where appropriate Year 4 subtractraction with up to 4 digits.	Model process of exchange using Numicon, base ten and then move to PV counters. Use the phrase 'take and make' for exchange- see Y3 The calculation will be shown alongside the model chosen to see the connection Model Calculation	Children to draw pv counters and show their exchange—see Y3 The calculation will be shown alongside the model chosen to see the connection Model Calculation	This will lead to an understanding of subtracting any number including decimals.
Introduce decimal subtraction through context of money	Children to be encouraged to use counters to represent numbers and Ones Tenths Hundredths Thousandths 1 1 1 03 03 00 000 000 000 000 000 000 0	52.7 - 27.9 tens ones ones tens ones tens ones ones tens ones ones tens ones ones	Rule 2 drop it down! No down of the 14 - 15.1 Value of 1.4

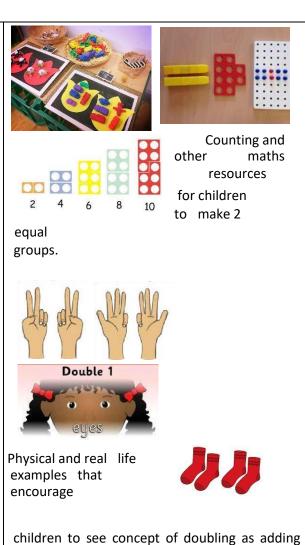
	agual to take take away loss minus subta	act laguar distance between how many many how	ı v many fewer/less than, most, least count back, how
Vocabulary			many rewerriess man, most, least count back, now
many left, how much less isdifference, count on, strategy, partition, tens units			

	Subtraction- Year 5/6					
Objective and S	Strategy	Concrete	Pictorial	Abstract		

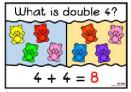
Subtract with at least 4 digits, including money and measures. Subtract with increasingly large and more complex numbers and decimal values (up to 3 decimal place).	See Year 4	See Year 4		71	3 10 8 9 6 0 8 5 8 6	, '6 , 9 , 7	9 4 5 3 3	9 9 0 1 8 3	9 0 9,	kg kg
Vocabulary	equal to, take, take-away, less, minus, subtract, leaves, dist left, how much less isdifference, count on, strategy, part	· · · · · · · · · · · · · · · · · · ·	less 1	than, mo	st, leas	t cou	int ba	ck, ho	ow mo	

	Multiplication-EYFS				
Objectives	Concrete	Pictorial	Abstract		





two equal groups.







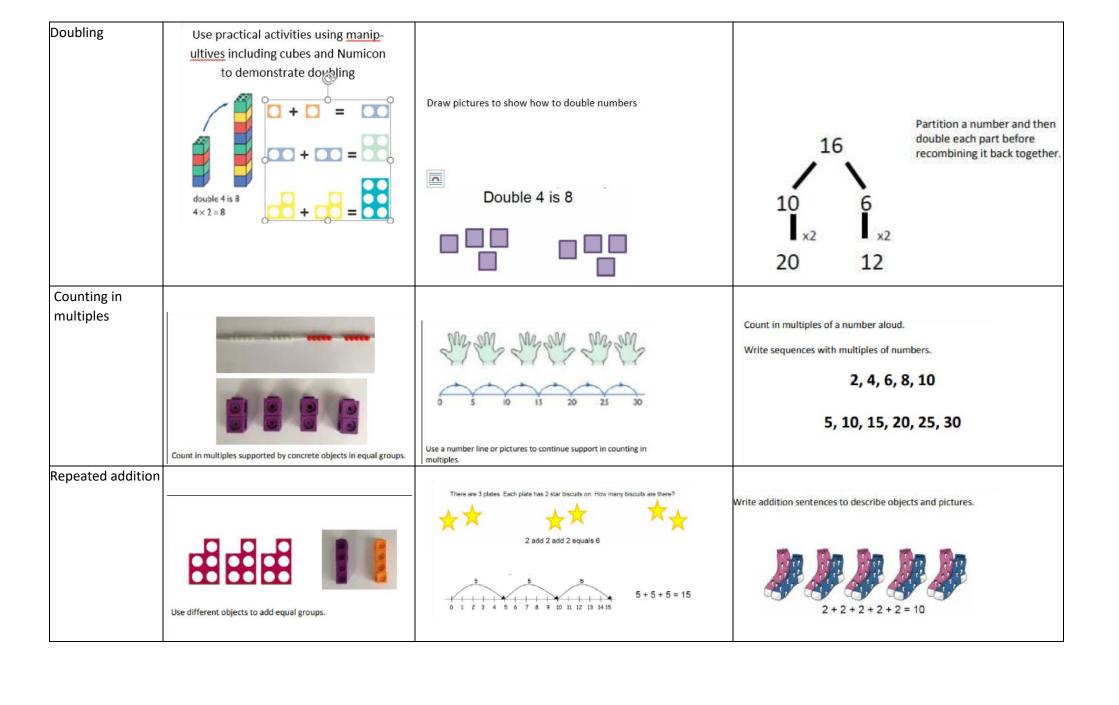


Pictures and icons that encourage children to see concept of doubling as adding two equal groups.

1+1=	7+7=
2+2=	8+8=
3+3=	9+9=
4+4=	10+10=
5+5=	11+11=
6+6=	12+12=

Addition calculations to model adding two equal groups.

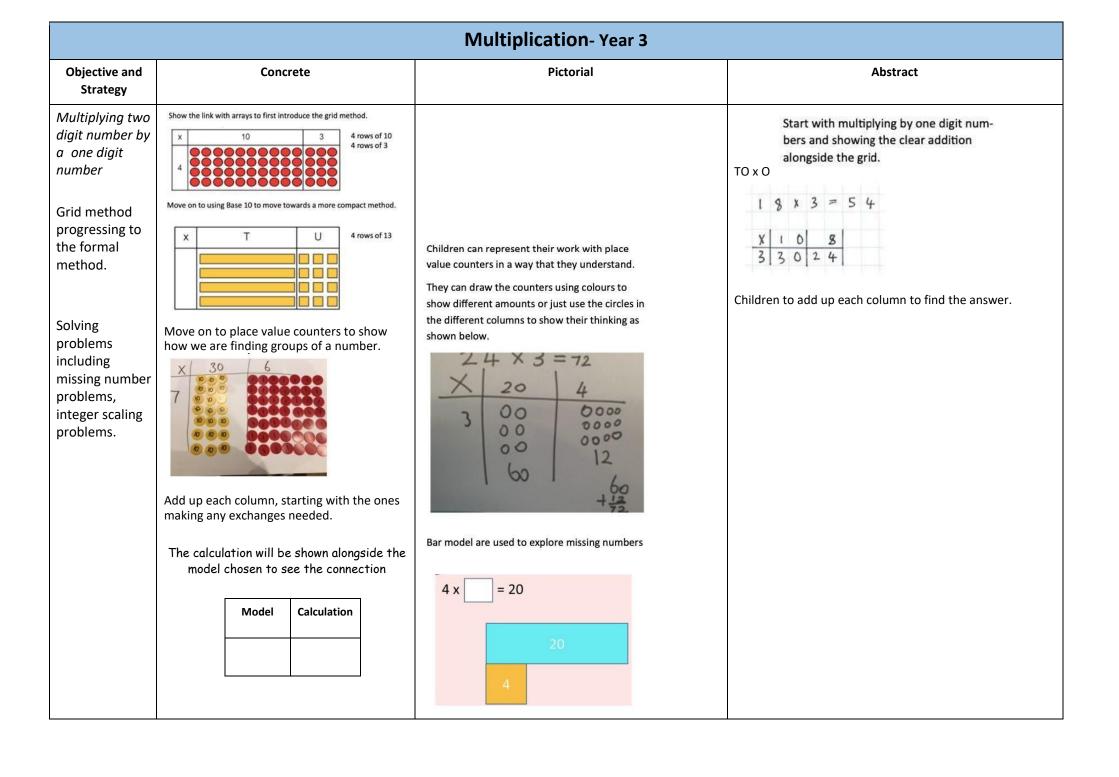
		Multiplication- Year 1	
Objective and	Concrete	Pictorial	Abstract
Strategy			



		Use pictorial including number lines to solve problems are 3 sweets in one bag. How many sweets are in 5 bags altogether? 3+3+3+3+3 = 15	
Understanding arrays	Use objects laid out in arrays to find the answers to 2 lots 5, 3 lots of 2 etc.		3 x 2 = 6 2 x 5 = 10
Vocabulary	Groups of, lots of, times, array, altogether, m ultip	ply	

		Multiplication- Year 2	
Objective and Strategy	Concrete	Pictorial	Abstract
Counting in multiples of 2, 3, 4, 5, 10 from 0 (repeated addition)	Count the groups as children are skip counting, children may use their fingers as they are skip counting. Use bar models. $5+5+5+5+5+5+5+5=40$	Number lines, counting sticks and bar models should be used to show representation of counting in multiples.	Count in multiples of a number aloud. Write sequences with multiples of numbers. 0, 2, 4, 6, 8, 10 0, 3, 6, 9, 12, 15
Multiplication	?	3 3 3 3	0, 5, 10, 15, 20, 25, 30 4 × 3 =
is commutative	Create arrays using counters and cubes and Numicon.	Use representations of arrays to show different calculations and explore commutativity.	12 = 3 × 4 12 = 4 × 3 Use an array to write multiplication sentences and reinforce repeated addition.
	Pupils should understand that an array can represent different equations and that, as multiplication is commutative, the order of the multiplication does not affect the answer.	0000	5+5+5=15 3+3+3+3+3=15 5 x 3 = 15 3 x 5 = 15

Using the Inverse This should be taught alongside division, so pupils learn how they work alongside each other. Vocabulary Groups of, lots of, times, array, altogether, multiply, multiplied by, repeated addition, sets of, equal	2 x 4 = 8 4 x 2 = 8 8 ÷ 2 = 4 8 ÷ 4 = 2 8 = 2 x 4 8 = 4 x 2 2 = 8 ÷ 4 4 = 8 ÷ 2 Show all 8 related fact family sentences.
--	---



\	Vocabulary	Groups of, lots of, times, array, altogether, multiply, multiplied by, repeated addition, sets of, equal groups, times as big as, commutative, product, multiples of, scale	
		ир	

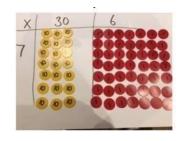
Multiplication- Year 4									
Objective and Strategy	Concrete	Pictorial	Abstract						

Multiply twodigit and three-digit numbers by a one-digit number using formal written layout

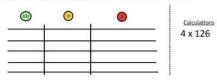
Grid method recap from year 3 for 2 digits x 1 digit

Multiplying

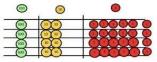
numbers by 1 digit (year 4 expectation)



Move on to place value counters to show how we are finding groups of a number. We are multiplying by 4 so we need 4 rows.



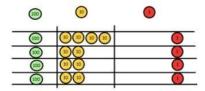
Fill each row with 126.



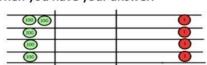
Add up each column, starting with the ones making any exchanges

Calculations

4 x 126

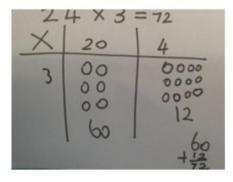


Then you have your answer.

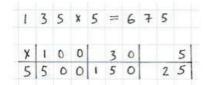


Children can represent their work with place value counters in a way that they understand.

They can draw the counters using colours to show different amounts or just use the circles in the different columns to show their thinking as shown below.

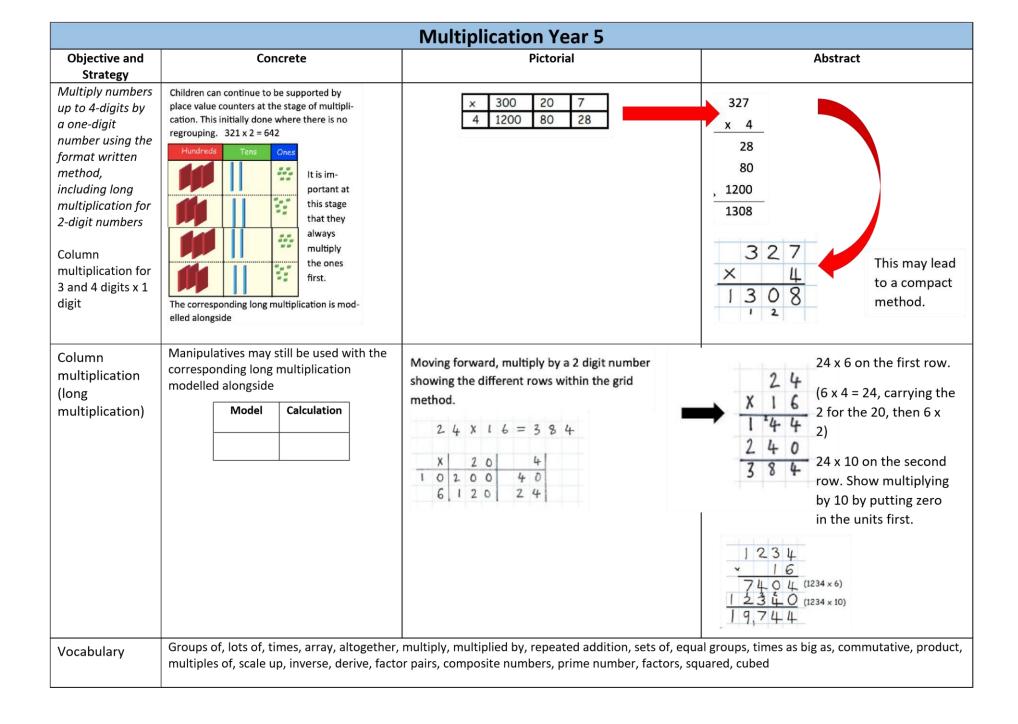


HTO x O



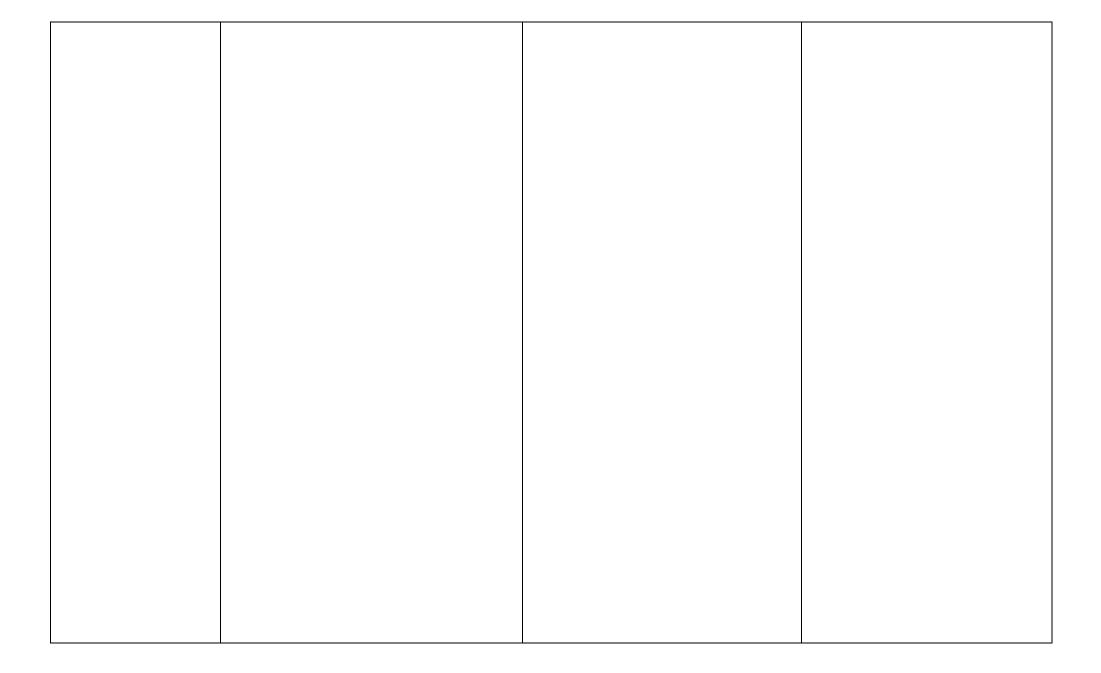
Children to add up each column to find the answer.

Column multiplication	Children can continue to be supported by place value counters at the stage of multipli-		d method to a forma	•	sed to show how this method.		1	2	4	X	5 =	
	cation. This initially done where there is no	×	100	20	4							
	regrouping. 321 x 2 = 642	5	500	100	20		1	2	4			
	Hundreds Tens Ones						X		5			
	It is im-							2	0	(4 ×	5)	
	portant at	50	59 59 59 59 59 59 59 59				1	0		(20 x		
	this stage	12.	1 31 31	- ?	10. 13. 13		5	0	0	(100×	5)	
	that they						6	, 2	0			
	always	= 8										
	multiply	8 × 60 - 8										
	the ones first.		× 6 = 48									
	first.	8	x 60 = 4	180	The Control of the Co		1	2	4	X	5	=
	The corresponding long multiplication is mod	48	480-8=472									
	elled alongside		odelling a	nd numb	per lines can support	-	1	2	4			
	Model Calculation	100 000 000 FEAT			AND	v	ı	_	7			This may lead
					roblems with multiplica- al written methods.	X	10	10	2			to a compact
		LIOII a	iongside t	ne iorina	a written methods.		6	.7	0			method.
						-						



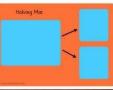
Objective and Strategy	Concrete	Pictorial	Abstract					
Multiply decimal up to 2 decimal place by a single digit.			Remind children that the single digit belongs in the units column. Line up the decimal points in the question and the answer.					
			3 · 1 9 × 8 2 5 · 5 2					
vocabulary	Groups of, lots of, times, array, altogether, multi multiples of, scale up, inverse, derive, factor pair		ts of, equal groups, times as big as, commutative, prod actors, squared, cubed					

Division- EYFS								
Objectives	Concrete	Pictorial	Abstract					
Solve problems including halving and sharing. • Halving a whole, halving a quantity of objects. • Sharing a quantity of objects.	Children have the opportunity to physically cut objects, food or shapes in half.	Pictures and icons that encourage children to see concept of halving in relation to subitising, addition and subtraction knowledge. i.e. Knowing 4 is made of 2 groups of 2, so half of 4 is 2. Bar model with pictures or icons to support understanding of finding 2 equal parts of a number, to further understand how two halves make a whole. Pictures for children to create and visualise 3 or more equal groups.						





Use visual supports such as halving mats and part part whole, with the physical objects and resources that can be manipulated.







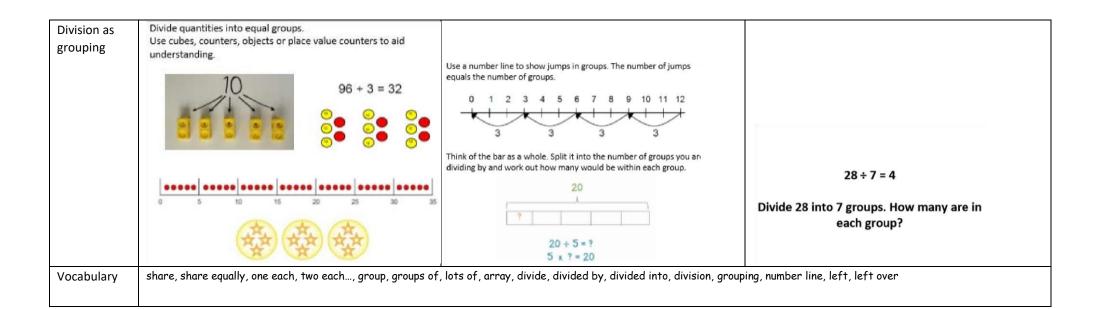
Counting and other maths resources for children to explore sharing between 3 or more.

Counting and other

maths resources for children to share into two equal groups.

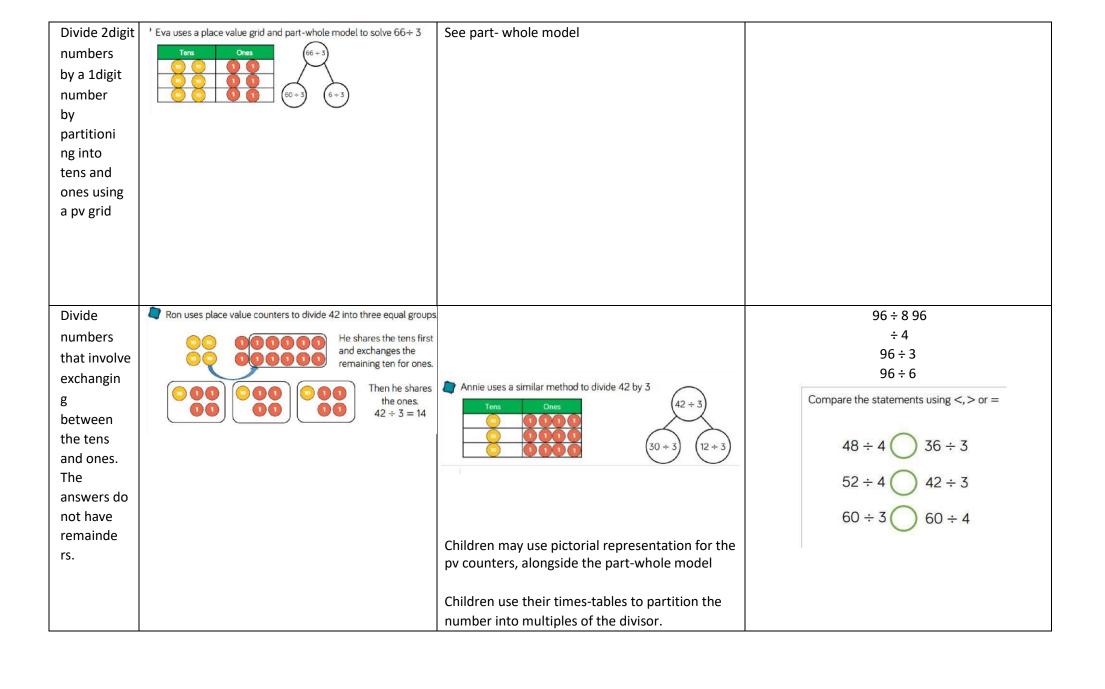
Division- Year 1				
Objective and Strategy	Concrete	Pictorial	Abstract	
Division as sharing (sharing objects into groups)	I have 10 cubes, can you share them equally in 2 groups?	Children use pictures or shapes to share quantities. $8 \div 2 = 4$ Children use bar modelling to show and support understanding.	Share 9 buns between three people. 9 ÷ 3 = 3	
Vocabulary	share, share equally, one each, two each, group, groups o	of, lots of, array		

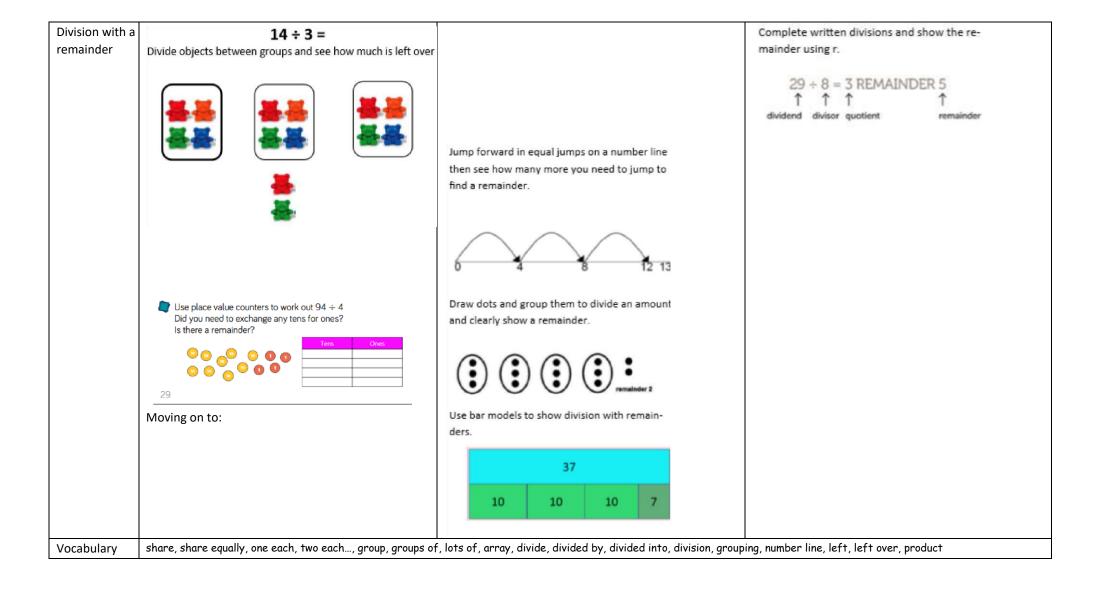
Division- Year 2			
Objective	Concrete	Pictorial	Abstract
and Strategy			

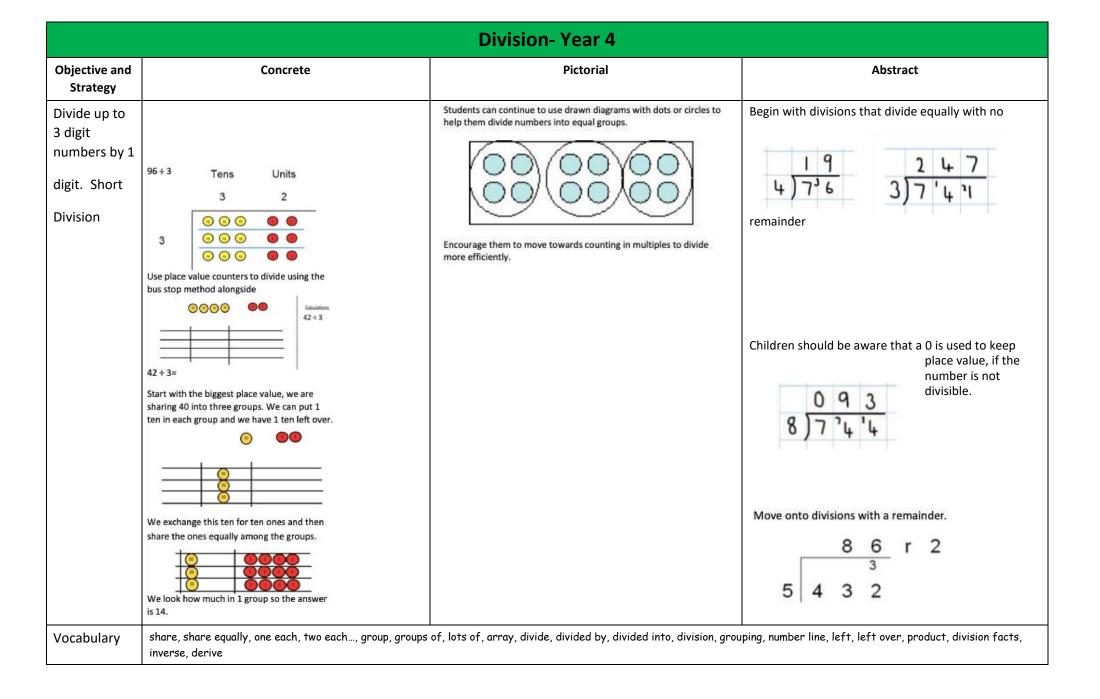


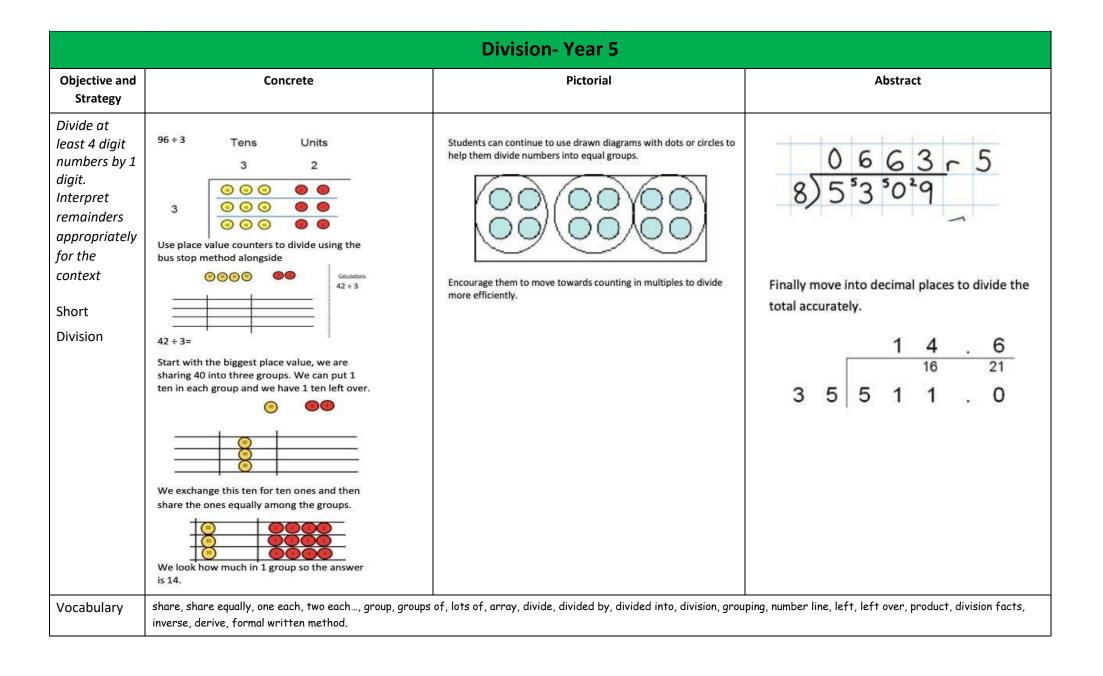
Division- Year 3			
Objective	Concrete	Pictorial	Abstract
and Strategy			

Division as Use cubes, counters, objects or place value How many groups of 6 in counters to aid understanding. grouping Continue to use bar modelling to aid solving 24? division problems. $24 \div 6 = 4$ 20 24 divided into groups of 6 = 4 $96 \div 3 = 32$ $20 \div 5 = ?$ 5 x ? = 20 Division Find the inverse of multiplication and division with arrays sentences by creating eight linking number sentences. $7 \times 4 = 28$ Draw an array and use lines to split the array into groups to make multiplication and division $4 \times 7 = 28$ sentences $28 \div 7 = 4$ Link division to multiplication by creating an $28 \div 4 = 7$ array and thinking about the number sentenc- $28 = 7 \times 4$ es that can be created. $28 = 4 \times 7$ Eg 15 ÷ 3 = 5 5 x 3 = 15 $4 = 28 \div 7$ 15 ÷ 5 = 3 3 x 5 = 15 $7 = 28 \div 4$









Division-Year 6	
Objective and Strategy	Abstract

Long Division

Step 1 – a remainder in the ones

- 4 does not go into 1 (hundred). So combine the 1 hundred with the 6 tens (160).
- 4 goes into 16 four times.
- 4 goes into 5 once, leaving a remainder of 1.

8 does not go into 3 of the thousands. So combine the 3 thousands with the 2 hundreds (3,200).

- 8 goes into 32 four times (3,200 + 8 = 400)
- 8 goes into 0 zero times (tens).
- 8 goes into 7 zero times, and leaves a remainder of 7.

When dividing the ones, 4 goes into 7 one time. Multiply $1 \times 4 = 4$, write that four under the 7, and subract. This finds us the remainder of 3.

Check: 4 × 61 + 3 = 247

When dividing the ones, 4 goes into 9 two times. Multiply $2 \times 4 = 8$, write that eight under the 9, and subract. This finds us the remainder of 1.

Check: $4 \times 402 + 1 = 1,609$

Step 2 – a remainder in the tens

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
t o	t o	t o
2)58	2)58	2 9 2) 5 <mark>8</mark>
	<u>- 4</u> 1	- 4 \ 1 <mark>8</mark>
Two goes into 5 two times, or 5 tens ÷ 2 = 2 whole tens but there is a remainder!	To find it, multiply 2 × 2 = 4, write that 4 under the five, and subtract to find the remainder of 1 ten.	Next, drop down the 8 of the ones next to the leftover 1 ten. You combine the remainder ten with 8 ones, and get 18.

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
t o	t o	t o
2 9 2) 5 8	292)58	2 9 2) 5 8
<u>-4</u>	<u>-4</u>	<u>-4</u>
18	<u>- 1 8</u>	<u>-18</u>
	0	0
Divide 2 into 18. Place 9 into the quotient.	Multiply 9 × 2 = 18, write that 18 under the 18, and subtract.	The division is over since there are no more digits in the dividend. The quotient is 29.

Step 3 – a remainder in any of the place values

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
1 2)278	2)278 -20	18 2)278 -2↓ 07
Two goes into 2 one time, or 2 hundreds + 2 = 1 hundred.	Multiply 1 × 2 = 2, write that 2 under the two, and subtract to find the remainder of zero.	Next, drop down the 7 of the tens next to the zero.
Divide.	Multiply & subtract.	Drop down the next digit.
13 2)278 -2 07 Divide 2 into 7. Place 3 into the	h t o 1 3 2) 2 7 8 -2 0 7 -6 1 Multiply 3 × 2 = 6, write that 6 under	2)278 -2 07 -6 18 Next, drop down the 8 of the ones
quotient.	the 7, and subtract to find the remainder of 1 ten.	next to the 1 leftover ten.
1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
13 <mark>9</mark> 2)278 -2 07 -6 18	139 2)278 -2 07 -6 18 -18	139 2)278 -2 07 -6 18 -18
Divide 2 into 18. Place 9 into the quotient.	Multiply 9 × 2 = 18, write that 18 under the 18, and subtract to find the remainder of zero.	There are no more digits to drop down. The quotient is 139.

Divide numbers up to 4 digits by a twodigit whole number using the formal written method of division	$ \begin{array}{c cccccccccccccccccccccccccccccccccc$
Vocabulary	share, share equally, one each, two each, group, groups of, lots of, array, divide, divided by, divided into, division, grouping, number line, left, left over, product, division facts, inverse, derive, formal written method.

Minimal Resources required to support the CPA approach (depending on year group):

- 10 frames (including egg boxes)
- Straws/pipe cleaners
- Bead strings (to 20 and 100)
- Base 10/Dienes
- Place value grids
- Double-sided counters
- Part-part whole templates
- Place value counters (KS2)
- Multi-link cubes